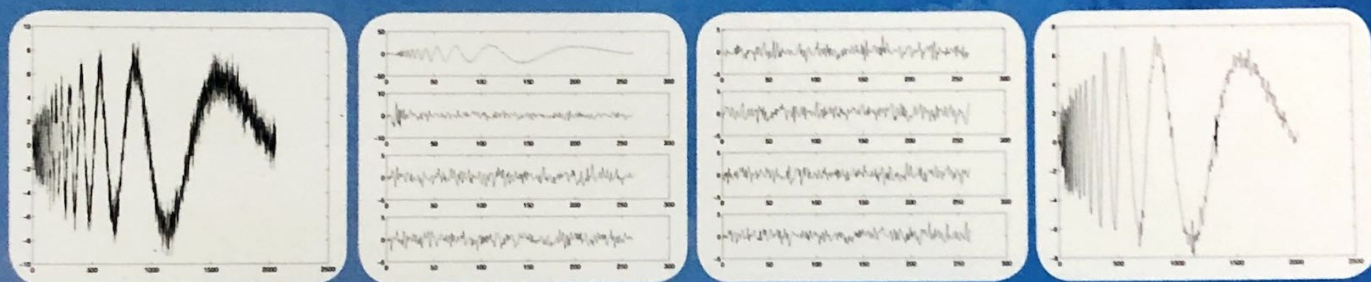


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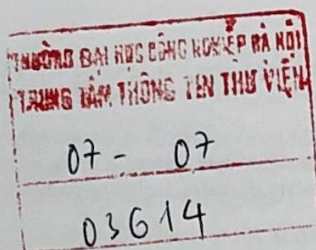
Principles, Algorithms
and System Design



**Winser Alexander
Cranos Williams**



Digital Signal Processing: Principles, Algorithms and System Design



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